

D.N.R.COLLEGE, (AUTONOMOUS): BHIMAVARAM
DEPARTMENT OF MANAGEMENT STUDIES



Quantitative Techniques in Management
I SEMESTER

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ONE-Way classification - ANOVA

129) Three samples each size of 5 were drawn from uncorrelated normal populations. Test the hypothesis that the population means are equal to 5 percent level.

Sample 1: 10 12 9 16 13

Sample 2: 9 7 12 11 11

Sample 3: 14 11 15 14 16

Sol: H_0 : Population means are equal

Sample 1 x_1	x_1^2	Sample 2 x_2	x_2^2	Sample 3 x_3	x_3^2
10	100	9	81	14	196
12	144	7	49	11	121
9	81	12	144	15	225
16	256	11	121	14	196
13	169	11	121	16	256
$\Sigma x_1 = 60$	$\Sigma x_1^2 = 750$	$\Sigma x_2 = 50$	$\Sigma x_2^2 = 516$	$\Sigma x_3 = 70$	$\Sigma x_3^2 = 994$

~~Sum of squares~~

OR

$$T = \sum x_1 + \sum x_2 + \sum x_3$$

$$= 60 + 50 + 70$$

$$= 180$$

$$\text{Correction factor} = \frac{T^2}{n}$$

$$= \frac{(180)^2}{15}$$

$$= \frac{32400}{15}$$

$$= 2160$$

Total sum of squares (SST) =

$$\sum x_1^2 + \sum x_2^2 + \sum x_3^2 - \frac{T^2}{n}$$

$$= 750 + 516 + 994 - 2160$$

$$= 2260 - 2160$$

$$= 100$$

Sum of squares between samples

$$SSB = \frac{(\sum x_1)^2}{n} + \frac{(\sum x_2)^2}{n} + \frac{(\sum x_3)^2}{n} - \frac{T^2}{n}$$

$$= \frac{(60)^2}{5} + \frac{(50)^2}{5} + \frac{(70)^2}{5} - 2160$$

$$= \frac{3600}{5} + \frac{2500}{5} + \frac{4900}{5} - 2160$$

$$= 720 + 500 + 980 - 2160$$

$$= 2200 - 2160$$

$$= 40$$

Sum of squares

with samples

$$SSW = SST - SSB$$

$$SSW = 100 - 40 = 60$$

ANOVA Table

Source of variation	Sum of squares (SS)	Difference of freedom	MS	F ratio
Between	40	$5 - 3 = 2$	$40/2 = 20$	
Within	60	$15 - 3 = 12$	$60/12 = 5$	$\frac{20}{5} = 4$

Table for $v_1 = 2$ & $v_2 = 12$ at $0.05 = 3.89$

Conclusion:

H_0 is rejected which means the population means of the three samples do not have the same

Two-way Classification - ANOVA:

2) A large scale manufacturing company has appointed managers with different educational qualification in its newly opened branches in three regions. Is there significant difference between & within the managers in terms of scale (Rs. '000)

Qualification	Regions			Total
	A	B	C	
MBA	10	12	11	33
CA	8	7	9	24
B.Tech	6	8	9	23
Total	24	27	29	80

Sol:

H_0 : Sales performance is equal between and within managers

Let denote A, B & C regions as x_1 , x_2 & x_3 respectively

Managers	Regions						Total
	x_1	x_1^2	x_2	x_2^2	x_3	x_3^2	
MBA	10	100	12	144	11	121	33
CA	8	64	7	49	9	81	24
B.Tech	6	36	8	64	9	81	23
	24	220	27	257	29	283	80

	MBA	x_1^2	CA	x_2^2	B.Tech	x_3^2
A	10	100	12	144	11	121
B	8	64	7	49	9	81
C	6	36	8	64	9	81
	33		24		23	

$$T = \sum x_1 + \sum x_2 + \sum x_3 = 24 + 27 + 29 = 80$$

The correction factor

$$T^2/n = \frac{(80)^2}{9} = \frac{6400}{9} = 711.11$$

The total sum of squares

$$\begin{aligned} SST &= \sum x_1^2 + \sum x_2^2 + \sum x_3^2 - \frac{T^2}{n} \\ &= 220 + 257 + 283 - 711.11 \\ &= 48.89 \end{aligned}$$

The sum of squares
between managers

$$\begin{aligned} SSB &= \frac{(33)^2}{3} + \frac{(24)^2}{3} + \frac{(23)^2}{3} - 711.11 \\ &= 363 + 192 + 176.33 - 711.11 \\ &= 20.22 \end{aligned}$$

The sum of squares
within managers

$$\begin{aligned} &= \frac{(24)^2}{3} + \frac{(27)^2}{3} + \frac{(29)^2}{3} - 711.11 \\ &= 192 + 243 + 280.33 - 711.11 \\ &= 4.22 \end{aligned}$$

The sum of squares of

residual

$$= SS_T - (SS_B + SS_W)$$

$$= 48.89 - (20.22 + 4.22)$$

$$= 24.45$$

ANOVA Table

Variation	SS	DF	MS
Between managers	20.22	2	10.11
Within managers	4.22	2	2.11
Residual	24.45	4	6.11

$10.11 / 6.11 = 1.65$
 $2.11 / 6.11 = 0.34$

For $F(0.05)$ [for $v_1 = 2, v_2 = 4$] = 6.94

Since the calculated value of F ratio is less than the table value, difference is insignificant. Hence, H_0 is accepted.

Test of goodness of fit - Chi square Test:

3) We can test if a worker is equally prone to producing defective components throughout an eight-hour shift (or) not. We break the shift into four 2-hour slots & count the

number of defective components produced in each of this slot. At the end of one-week found that the worker has produced 50 defective components with the following breakup

Time slot (Hours)	Observed frequency
8.00 - 10.00	8
10.00 - 12.00	11
12.00 - 14.30	16
14.30 - 16.30	15
	50

Is it reasonable to assume that the probability to produce a defective component equal in each of the four 2-hour slots?

Sol:

Let denote probability of defective component came from the i th slot by p_i

$$H_0: p_1 = p_2 = p_3 = p_4 = 0.25$$

$H_1: \text{All of } p_1, p_2, p_3 \text{ \& } p_4 \text{ are not equal}$

Calculate the expected frequency based on the assumption that the null hypothesis is true. It means the average expected frequency per slot become $12.5 (50/4)$

Timeslot	Observed frequency (O)	Expected frequency (E)	$(O-E)^2/E$
8.00-10.00	8	12.50	$(8-12.50)^2/8 = 1.62$
10.00-12.00	11	12.50	$(11-12.50)^2/11 = 0.18$
12.00-14.30	16	12.50	$(16-12.50)^2/16 = 0.98$
14.30-16.30	15	12.50	$(15-12.50)^2/15 = 0.50$
	50	50.00	3.28

$$\chi^2 = 3.28$$

$$\chi^2 = \sum \frac{(O-E)^2}{E} = 3.28$$

$$d.f = 7.815$$

The calculated value of chi-square is less than the table value. It means the difference is insignificant. Hence H_0 is accepted.

Test of Independence of Attributes:

- ④ A survey of industrial sales persons included questions on the age of respondents and the degree of job pressure on the sales persons felt in connection with the job. Data is presented below. Using a significance level of 0.01, examine if there is any relationship between age & degree of job pressure.

Age (Years)	Degree of job pressure		
	Low	Medium	High
Less than 25	32	25	17
25-34	22	19	20
35-54	17	20	25
Above 55	15	24	26

Sol:

Age years	Degree of job pressure			Total
	Low	Medium	High	
less 25 (24.29) (24.29)	32 (24.85) (24.85)	25 (24.86) (24.86)	17 ? ?	74
25-34 (20.02) (20.02)	22 (20.49) (20.49)	19 (20.49) (20.49)	20 ? ?	61
35-54 (20.35) (20.35)	17 (20.82) (20.82)	20 (20.83) (20.83)	25 ? ?	62

Let us take the null hypothesis that there is no significant difference in the effectiveness of the two drugs. Applying χ^2 test

Sol: ~~Applying χ^2 test~~
 Ho: There is relationship b/w age & degree of Job pressure

Age (years)	Degree of Job pressure			Total
	Low	Medium	high	
less 25 (24.29)	32 (24.85)	25 (24.86)	17	74
25-34 (20.02)	22 (20.49)	19 (20.49)	20	61
35-54 (20.35)	17 (20.82)	20 (20.83)	25	62
Above 55 (21.34)	15 (21.84)	24 (21.82)	26	65
	86	88	88	262

By applying chi-square test formula

$$\chi^2 = \sum \frac{(O - E)^2}{E}$$

Ans. Arrange data in 4x3 contingency table

E values:

$$\frac{86 \times 74}{262} = 24.29, \quad \frac{86 \times 61}{262} = 20.02, \quad \frac{86 \times 62}{262} = 20.35$$

$$\frac{86 \times 65}{262} = 21.34, \quad \frac{88 \times 74}{262} = 24.85, \quad \frac{88 \times 61}{262} = 20.49$$

$$\frac{88 \times 62}{262} = 20.82, \quad \frac{88 \times 65}{262} = 21.84, \quad \frac{88 \times 74}{262} = 24.85$$

$$\frac{88 \times 61}{262} = 20.49, \quad \frac{88 \times 62}{262} = 20.83, \quad \frac{88 \times 65}{262} = 21.82$$

<u>O</u>	<u>E</u>	$(O-E)^2$	$(O-E)^2/E$
32	24.29	59.44	$259.44/24.29$ = 2.447
22	20.02	3.92	0.196
17	20.35	11.22	0.551
15	21.34	40.19	1.883
25	24.85	0.025	0.0009
19	20.49	2.22	0.108
20	20.82	0.67	0.032
24	21.84	4.66	0.214
17	24.86	61.77	2.485
20	20.49	0.69 0.24	0.012
25	20.83	17.4	0.835
26	21.82	17.5	0.800
			$\Sigma \left[\frac{(O-E)^2}{E} \right]$ = 9.56

Table value at 0.01 for 6 d.f

$$= 16.812$$

The calculated value of chi-square is less than table value. It implies difference not significant. Hence, H_0 is accepted.